



Parallel Implementation of Multivariate Empirical Mode Decomposition on GPU

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Zeyu Wang, Zoltan Juhasz

University of Pannonia
Veszprem, Hungary



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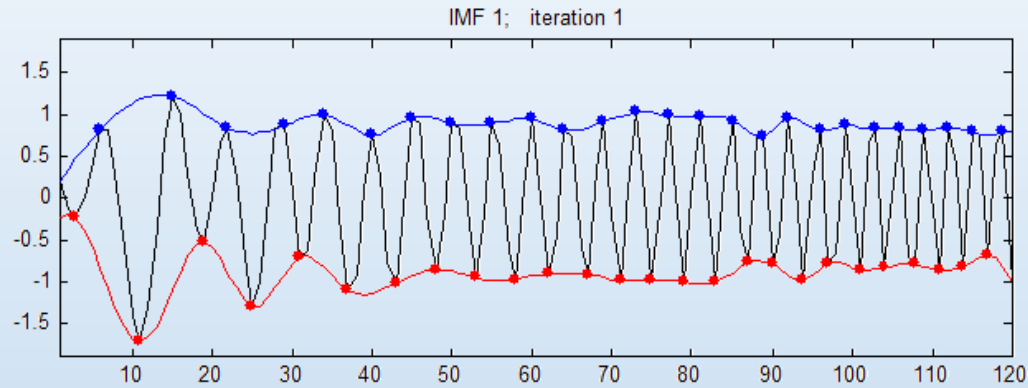
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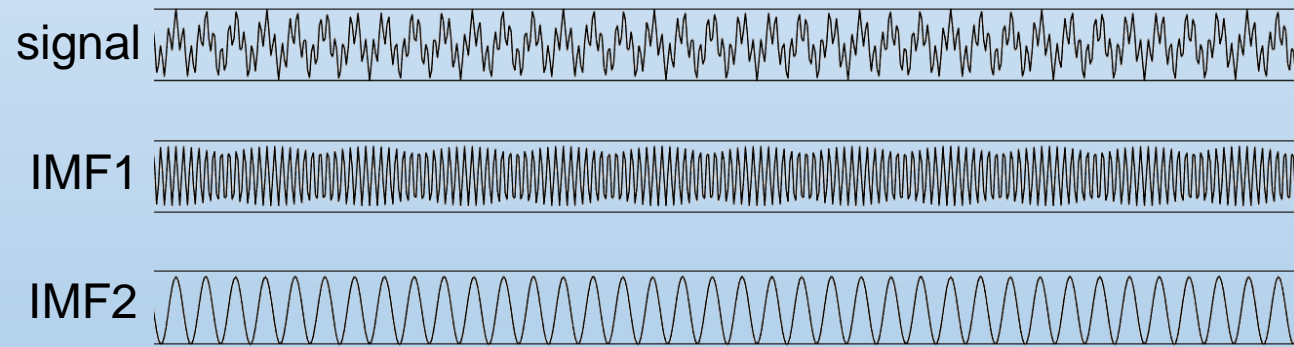
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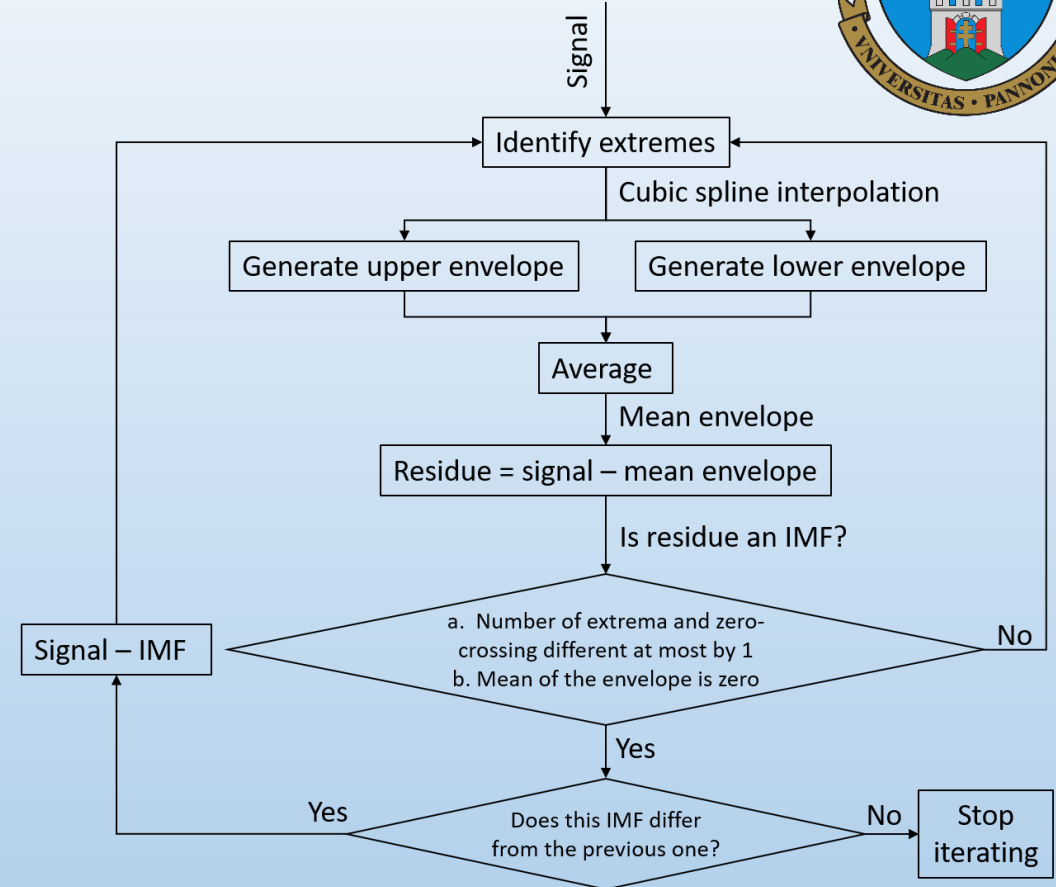
1.1 Empirical Mode Decomposition



EMD process



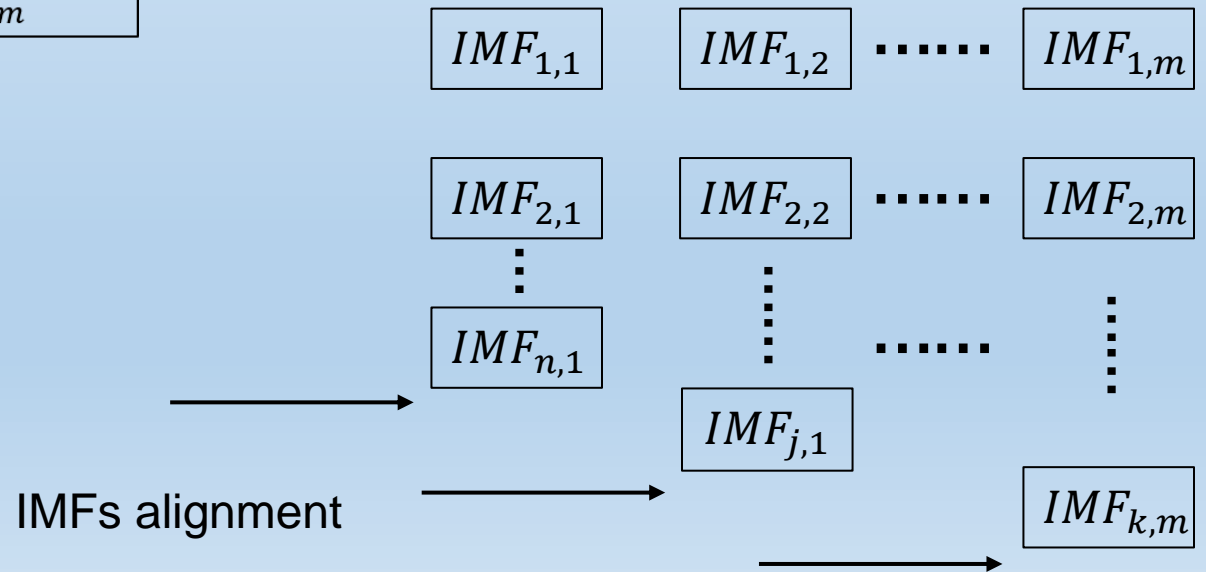
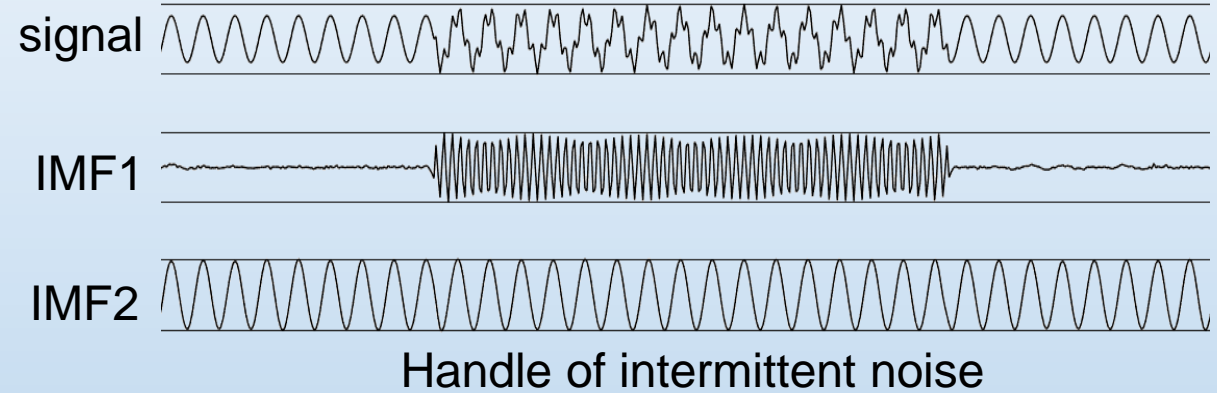
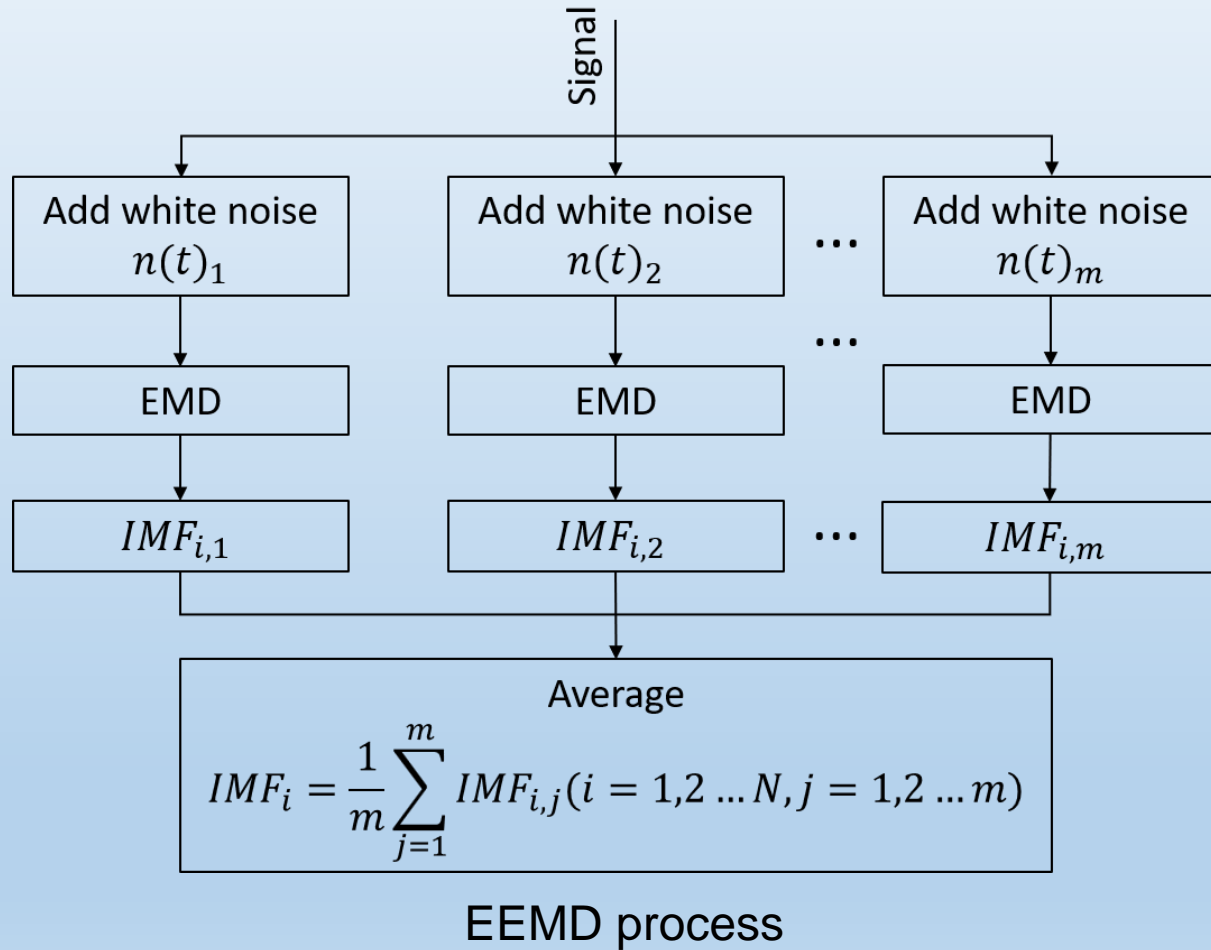
Separation of different oscillation modes



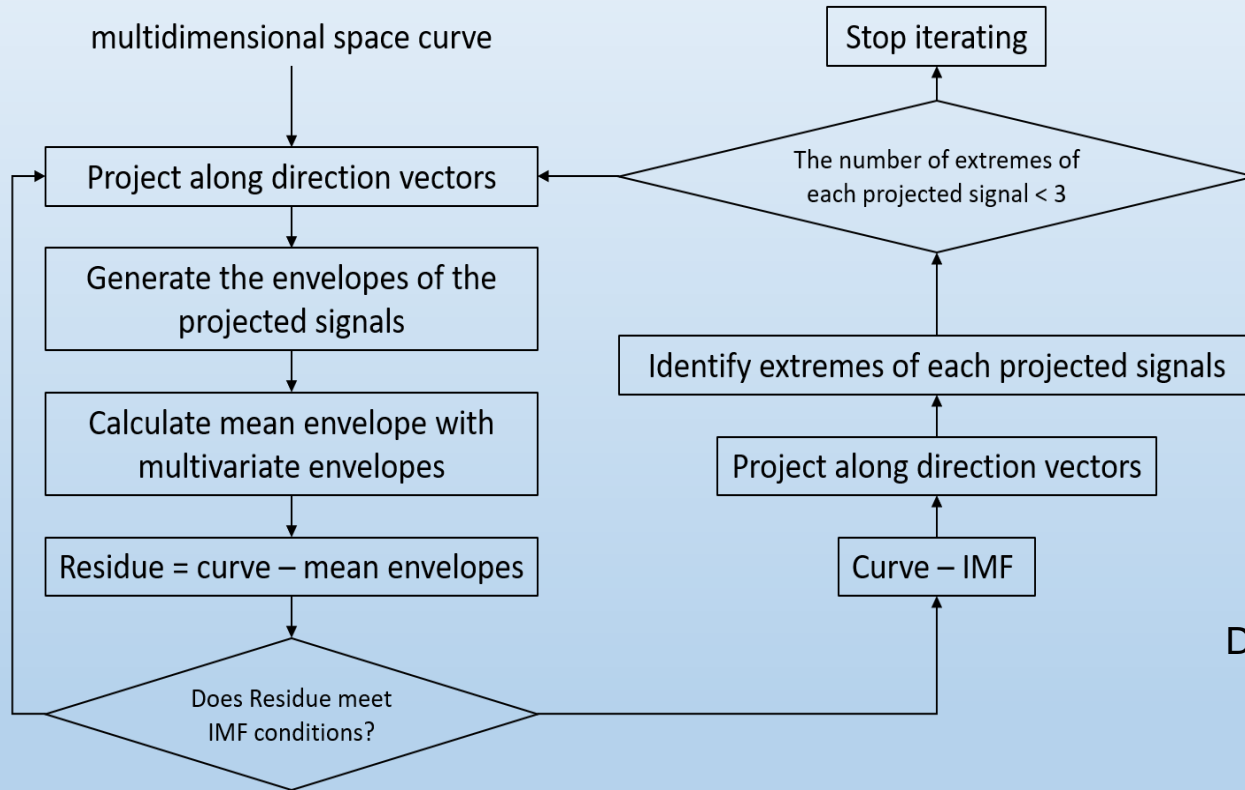
EMD process flowchart

N. E. Huang et al., "The empirical mode decomposition and the Hilbert spectrum for nonlinear and non-stationary time series analysis," Proc. R. Soc. A Math. Phys. Eng. Sci., vol. 454, no. 1971, pp. 903–995, 1998

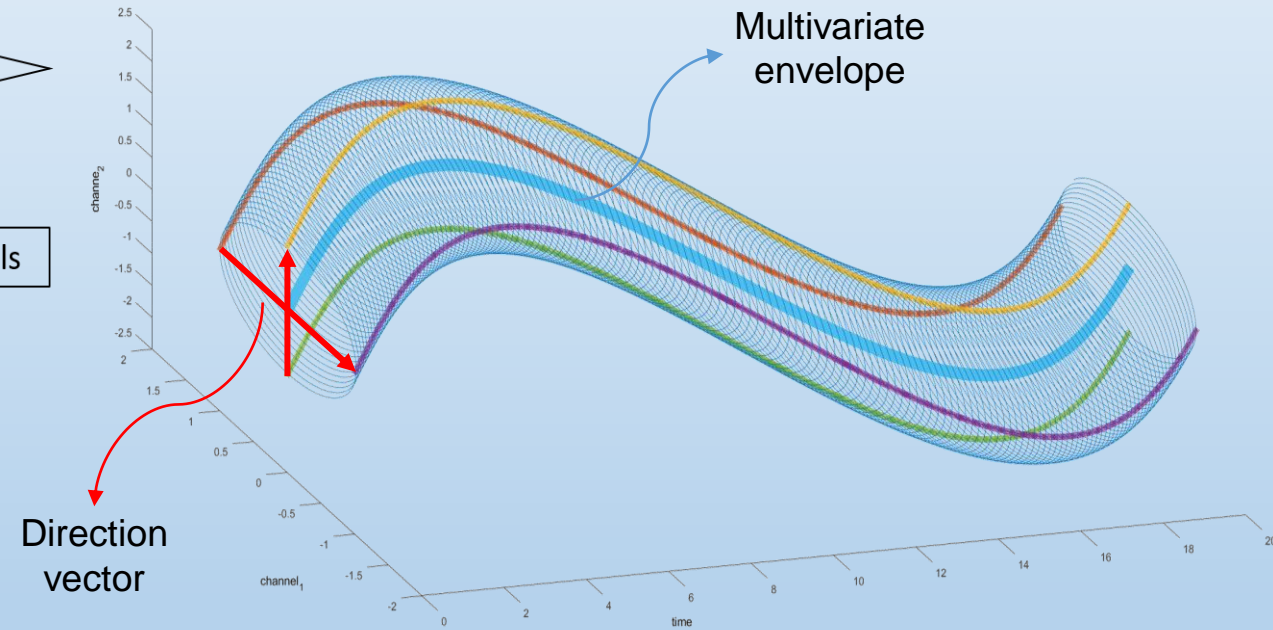
1.2 Features of EMD and its variants



1.3 Processing pipeline of MEMD



MEMD process flowchart

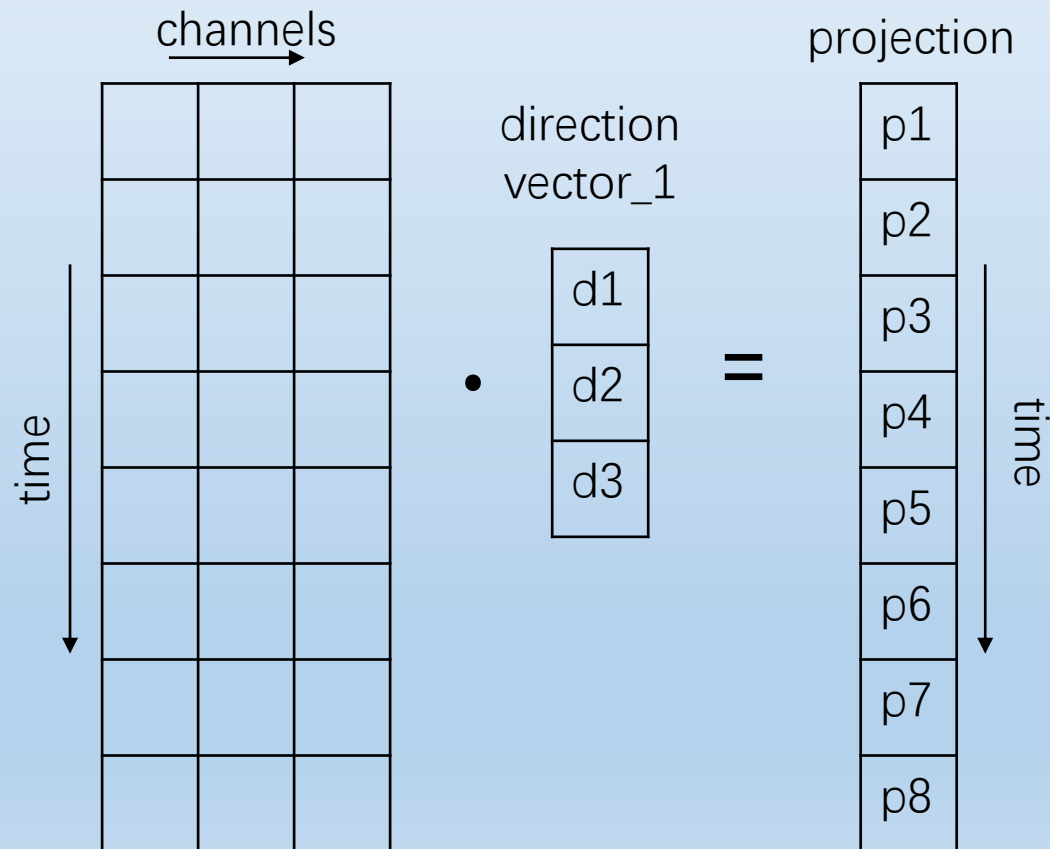


Envelopes of projected signals and the multivariate envelope

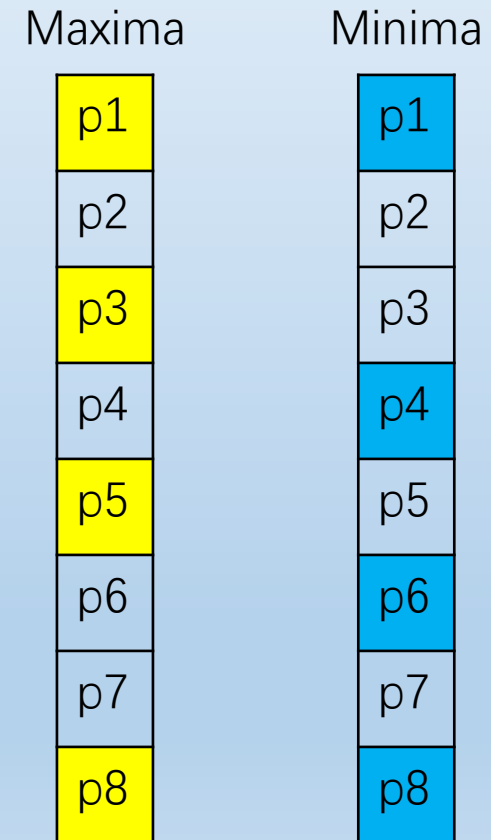
2.1 Numerical steps of MEMD



1. Use the data matrix to dot product the direct vector:



2. Detect the extreme points on the projection signal

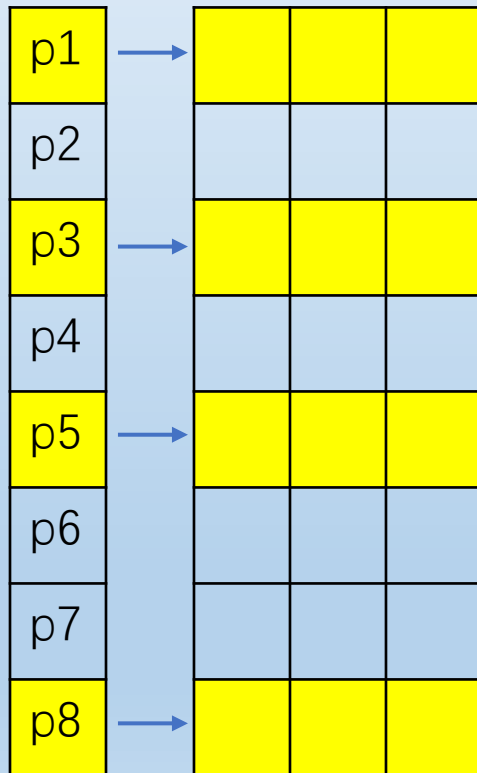


2.1 Numerical steps of MEMD

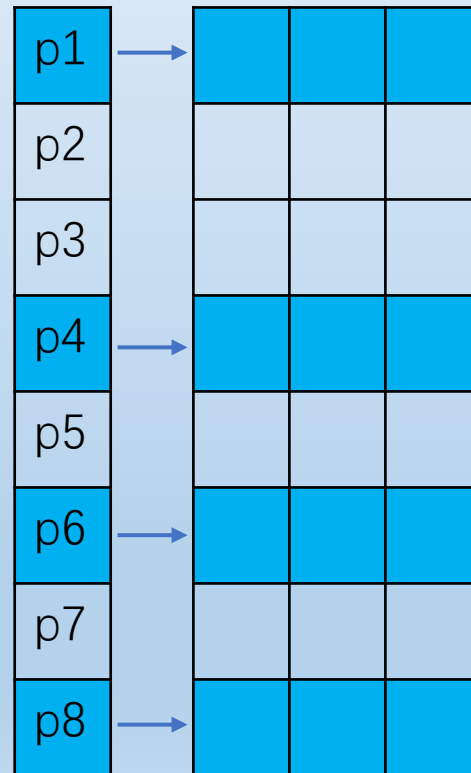


3. Find the corresponding multivariate extrema

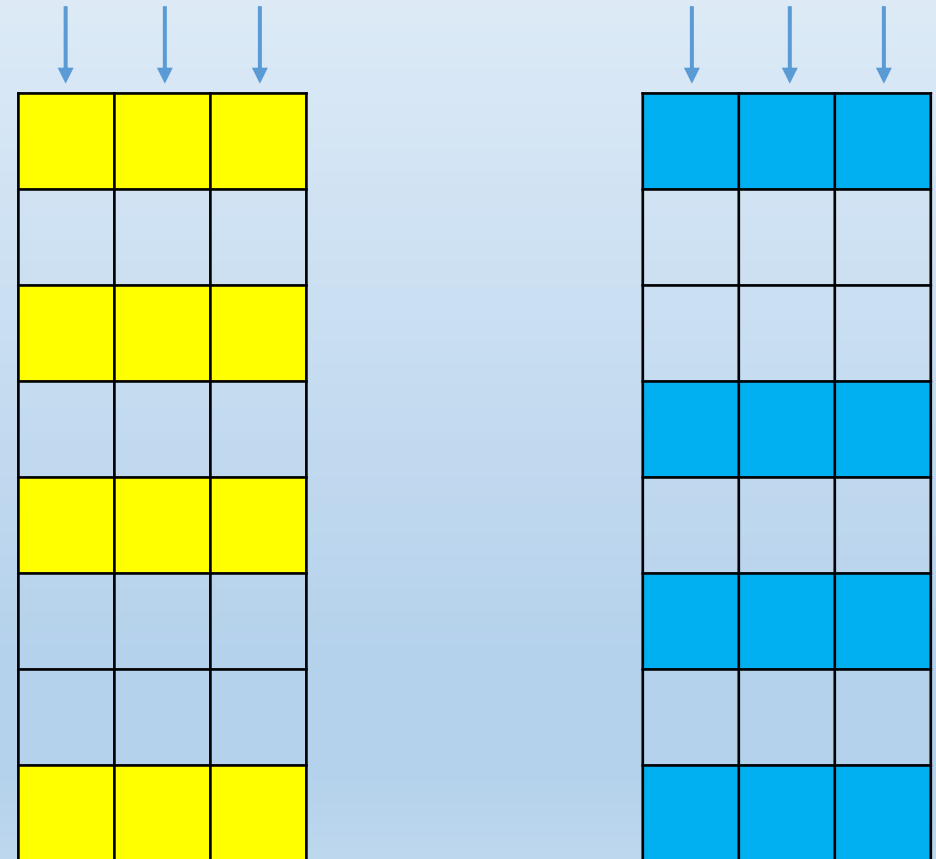
Maxima



Minima



4. Interpolate on the dimensions of multivariate extrema

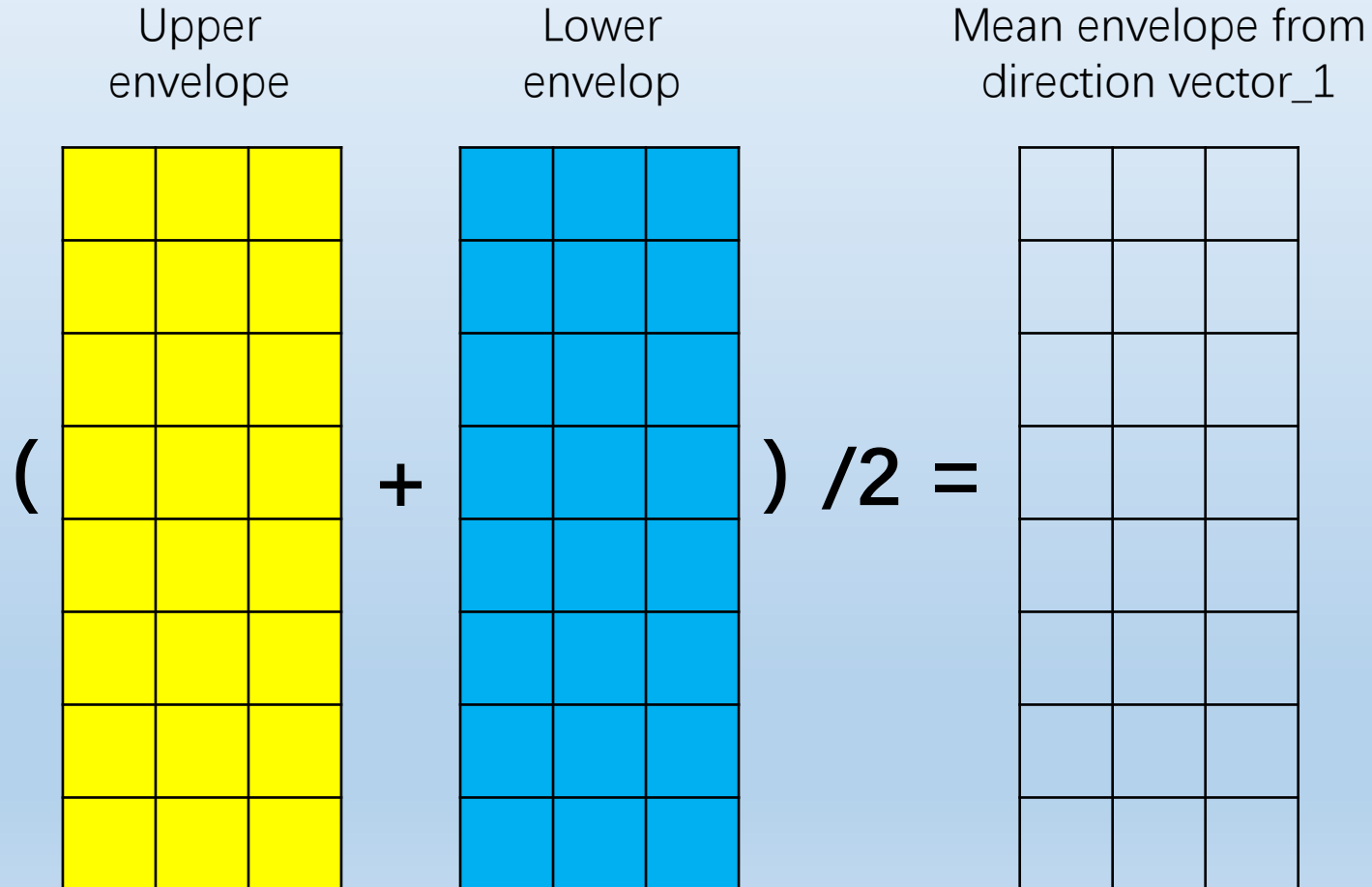


(Here we need to perform six interpolation operations)

2.1 Numerical steps of MEMD



5. Calculate multivariate mean envelope

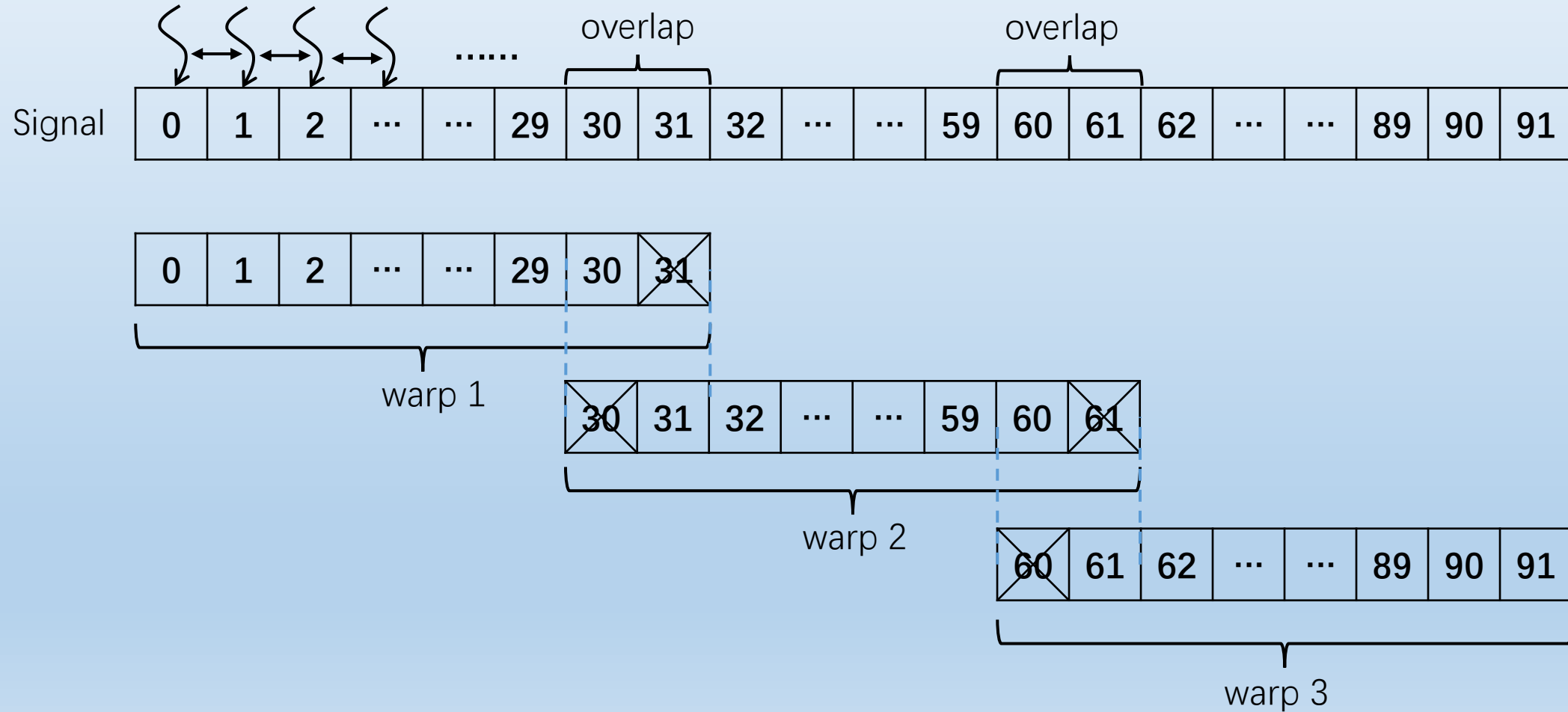


6. Calculates the mean envelope from the mean envelopes of all direction vectors.

2.2 Implementation details



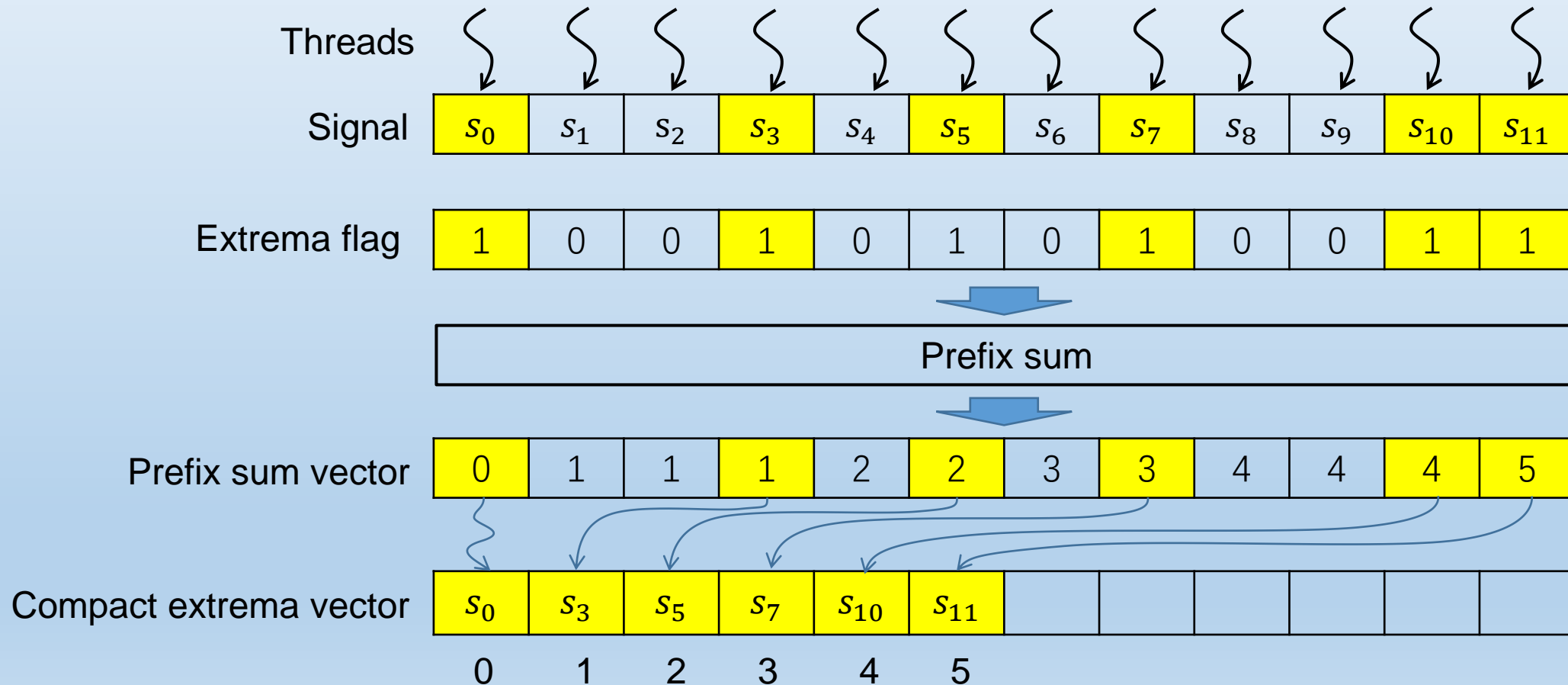
Use CUDA shuffle operation to detect extrema



2.2 Implementation details



Use prefix sum to get compact extrema vector

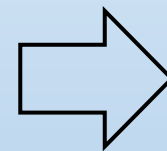
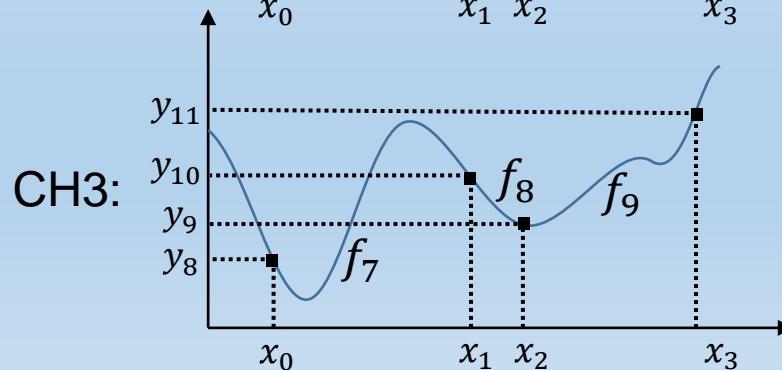
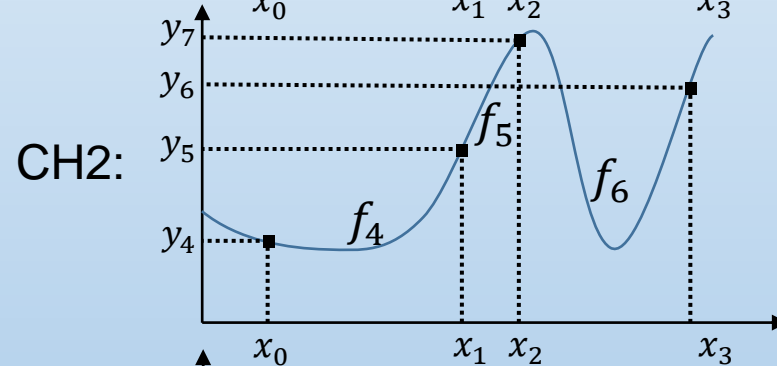
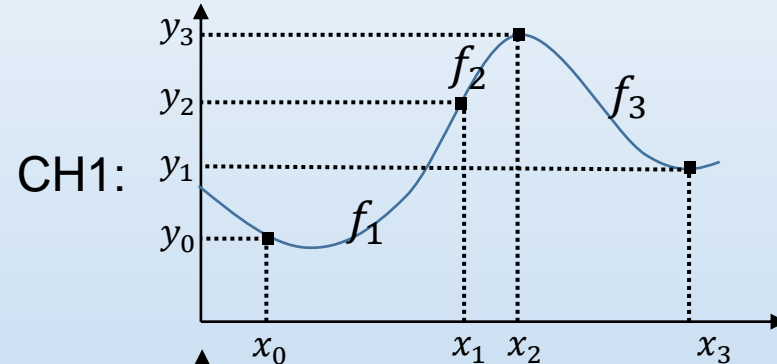


2.2 Implementation details



Multi tridiagonal systems solver in interpolation

| | | | |
|-------|-------|-------|----------|
| x_3 | y_3 | y_7 | y_{11} |
| | | | |
| x_2 | y_2 | y_6 | y_{10} |
| | | | |
| x_1 | y_1 | y_5 | y_9 |
| | | | |
| | | | |
| x_0 | y_0 | y_4 | y_8 |
| | CH1 | CH2 | CH3 |



$$\begin{bmatrix} b_1 & c_1 & & & 0 \\ a_2 & b_2 & c_2 & & \\ & a_3 & b_3 & \ddots & \\ & & \ddots & \ddots & c_{n-1} \\ 0 & & & a_n & b_n \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_n \end{bmatrix} =$$

Coefficient matrix

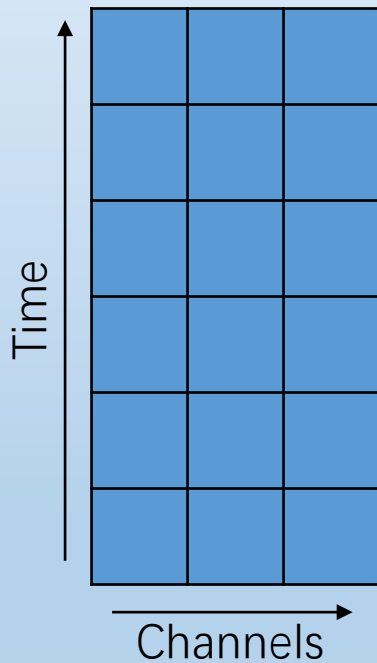
$$\begin{bmatrix} d_{11} & d_{21} & d_{31} \\ d_{12} & d_{22} & d_{32} \\ d_{13} & d_{23} & d_{33} \\ \vdots & \vdots & \vdots \\ d_{1n} & d_{2n} & d_{3n} \end{bmatrix} \text{ Right hand matrix}$$

CH1 CH2 CH3

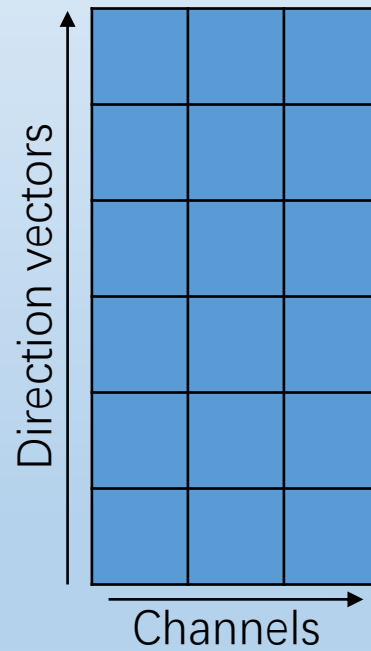
2.3 Data layout in memory



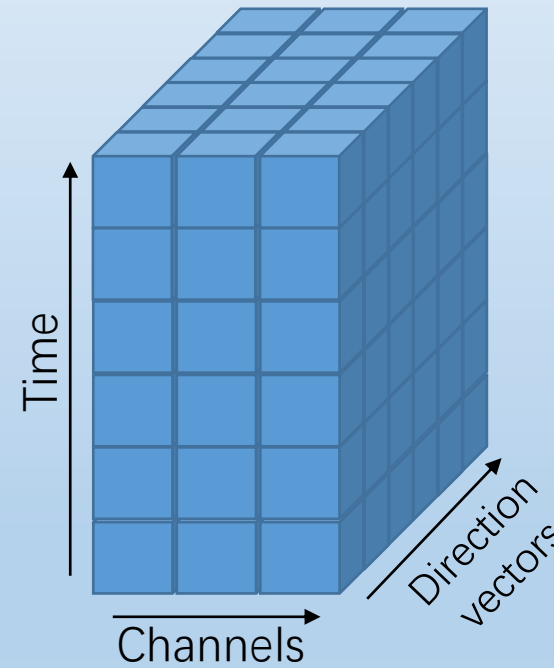
To store raw signal and multivariate IMF



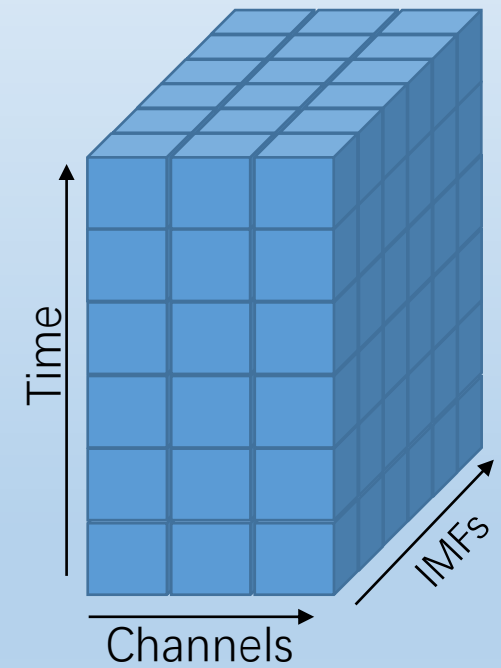
To store direction vectors



To store projected signals



To store IMFs result



X2

3.1 Performance overview



Dataset: EEGLAB sample dataset

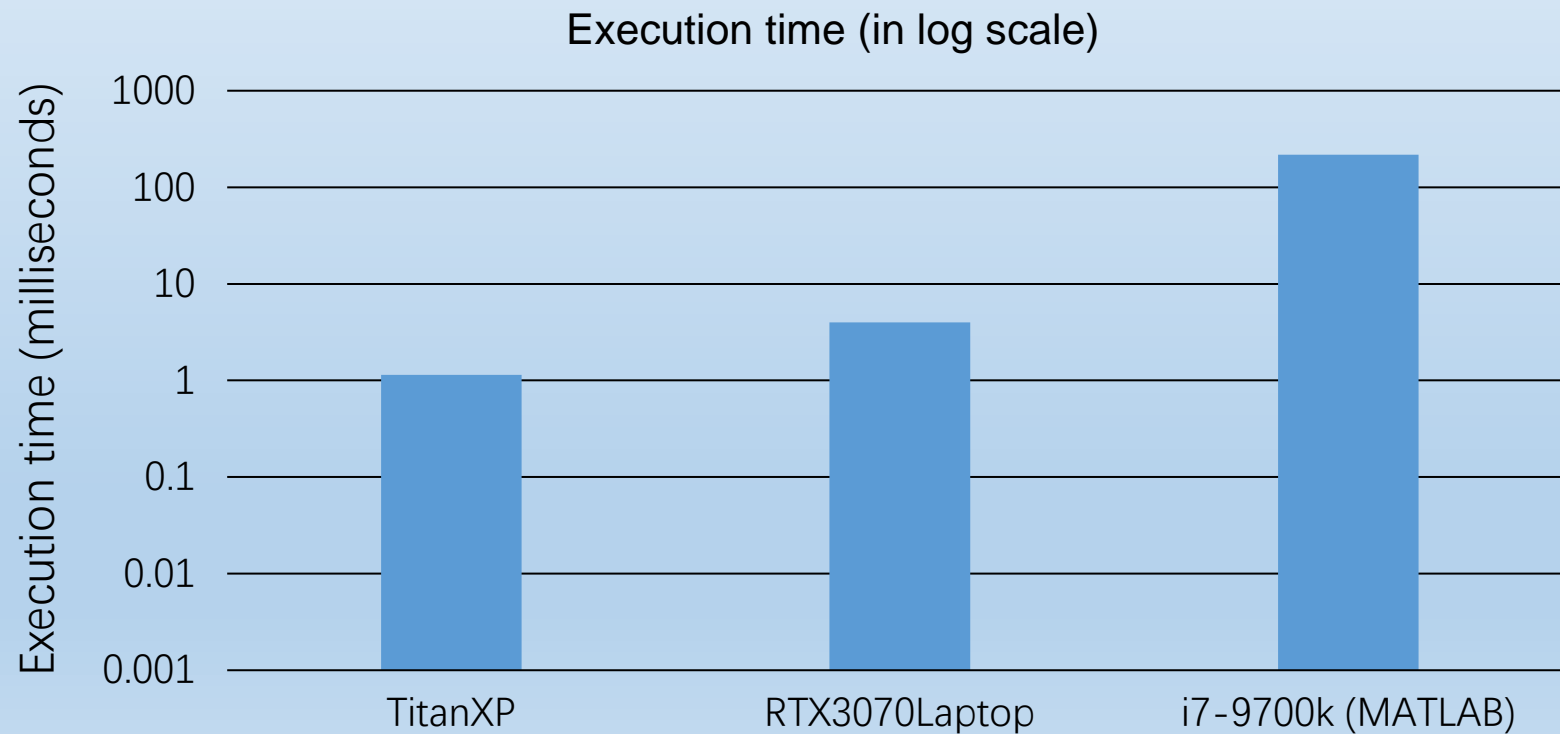
Number of channels: 4

Number of direction vectors: 64

Length of signal: 30504

Number of IMFs: 8

Number of iteration: 10



Compared to CPU,
Titan achieved **190X**
RTX3070 achieved **55X**
speedup

3.2 Kernel performance compared to literature



Number of channels: 16

Number of direction vectors: 64

Length of signal: 1001

Number of IMFs: 8

Number of iteration: 10

| Kernels | Number of calls | Execution time (μs) | | Speedup |
|------------------|-----------------|----------------------------------|-------------|---------|
| | | Literature [1] | Our version | |
| HammersleySeqGen | 1 | 11 | 3.42 | 3x |
| DirectionVecGen | 1 | 148 | 64.64 | 2x |
| Projections | 7 | 802 | 10.21 | 79x |
| PeaksDetection | 70 | 1232 | 6.61 | 187x |
| BoundaryCondSet | 140 | 3961 | 84.73 | 47x |
| EnvelopeMean | 140 | 152 | 28.34 | 5x |

[1] Mujahid, T., Rahman, A. U., & Khan, M. M. (2017). GPU-Accelerated Multivariate Empirical Mode Decomposition for Massive Neural Data Processing. *IEEE Access*, 5, 8691–8701.

4 Future works



1. There are still limitations in our performance tests, and in the future, we will test more datasets including 128-channel EEG signals under different execution parameters.
2. The effects of some detailed parameter settings on the decomposition results still need to be further studied, such as the settings of extrema and tridiagonal matrix boundary conditions, and the setting of sifting stop criterion.
3. Some numerical validations are currently ongoing, and the stream mechanism will be introduced into MEDM computations to further improve the parallelization and performance.